

# 단위 조작

## Unit operation

10.4 – 10.6

흡수탑에서의 물질전달

# 전달 법칙

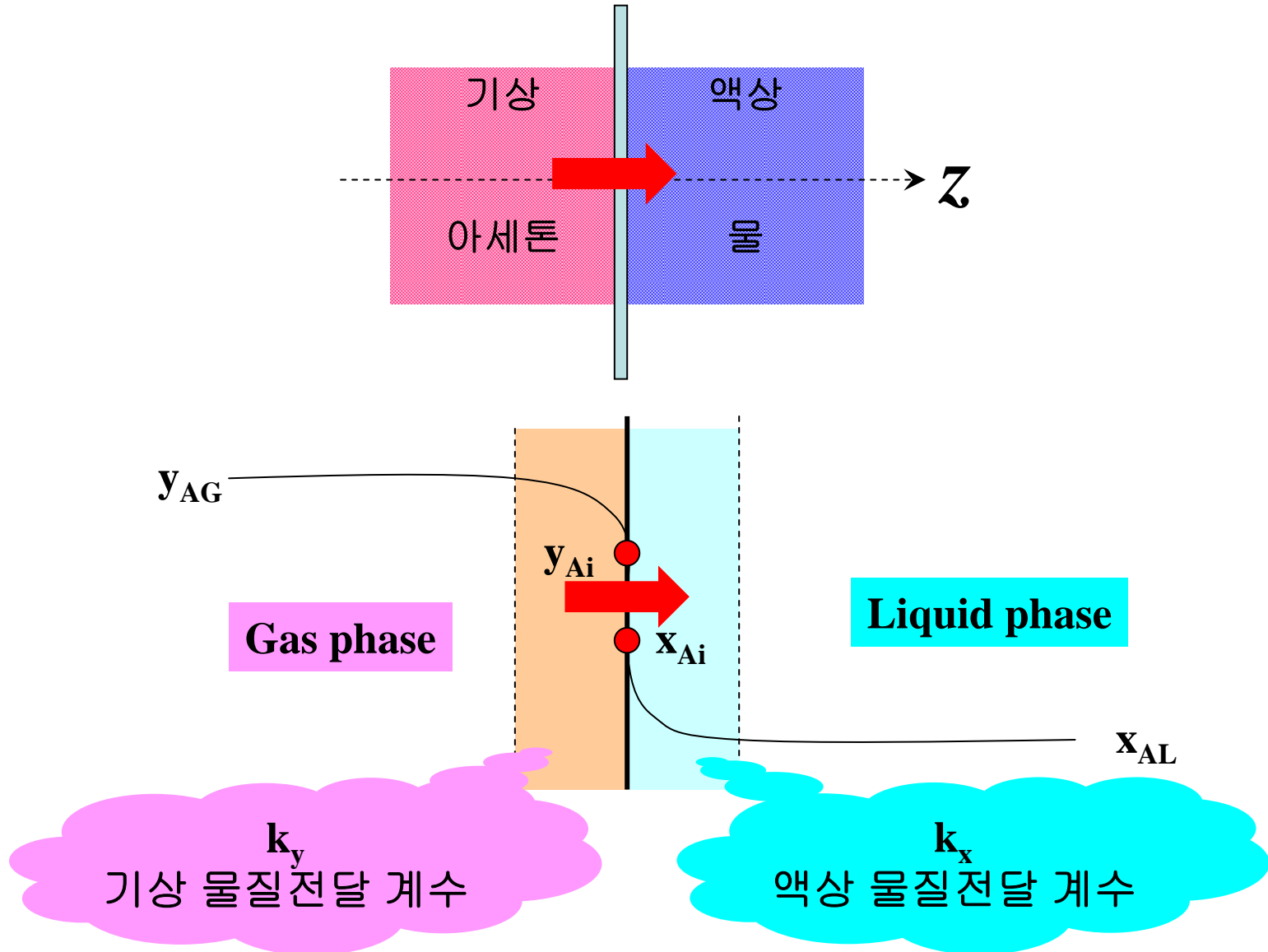
$$\text{전달속도} = \frac{\text{구동력}}{\text{저항}}$$

$$\text{heat flux} = \frac{\text{구동력}}{\text{저항}} = \frac{\text{온도차}}{\text{열전달계수의 역수}}$$

$$\text{mass flux} = \frac{\text{구동력}}{\text{저항}} = \frac{\text{농도차}}{\text{물질전달계수의 역수}}$$

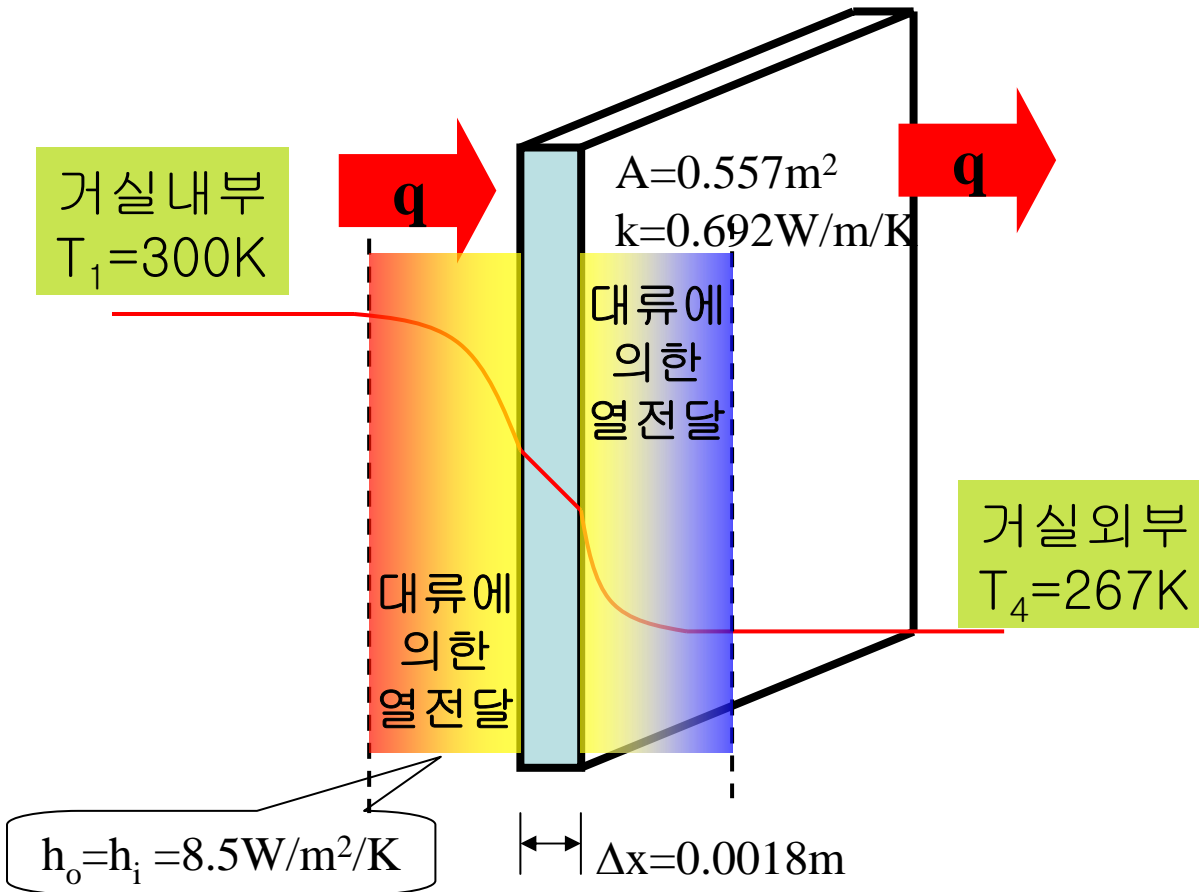
$$\text{mass flux} = \frac{\Delta C_A}{1/k_1 + 1/k_2 + 1/k_3}$$

# 10.4 두 상간의 물질전달



# 4.3D 총괄열전달 계수 (conduction+convection)

- 문제 4.3-6 유리창 내부에서 외부로의 열손실



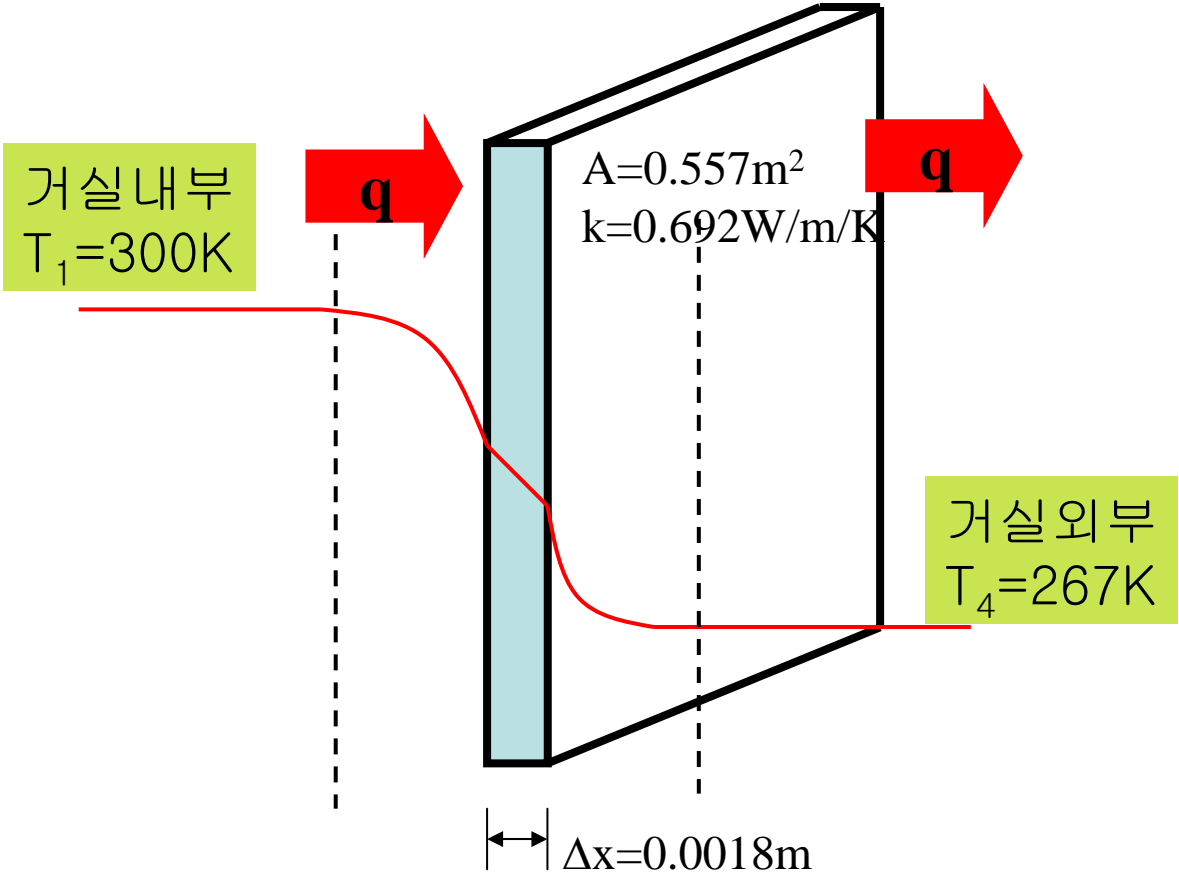
$$q = q_1 = q_2 = q_3$$

$$q_1 = h_i A (T_1 - T_2)$$

$$q_2 = kA \frac{(T_2 - T_3)}{\Delta x}$$

$$q_3 = h_o A (T_3 - T_4)$$

• 문제 4.3-6 유리창 내부에서 외부로의 열손실



$$q_1 = h_i A (T_1 - T_2)$$

$$q_2 = kA \frac{(T_2 - T_3)}{\Delta x}$$

$$q_3 = h_o A (T_3 - T_4)$$

$$(T_1 - T_2) = \frac{q}{h_i A}$$

$$(T_2 - T_3) = \frac{q}{kA / \Delta x}$$

$$(T_3 - T_4) = \frac{q}{h_o A}$$

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$$(T_1 - T_4) = \frac{q}{h_i A} + \frac{q}{kA / \Delta x} + \frac{q}{h_o A}$$

$$q = \frac{1}{\frac{1}{h_i A} + \frac{\Delta x}{kA} + \frac{1}{h_o A}} (T_1 - T_4)$$

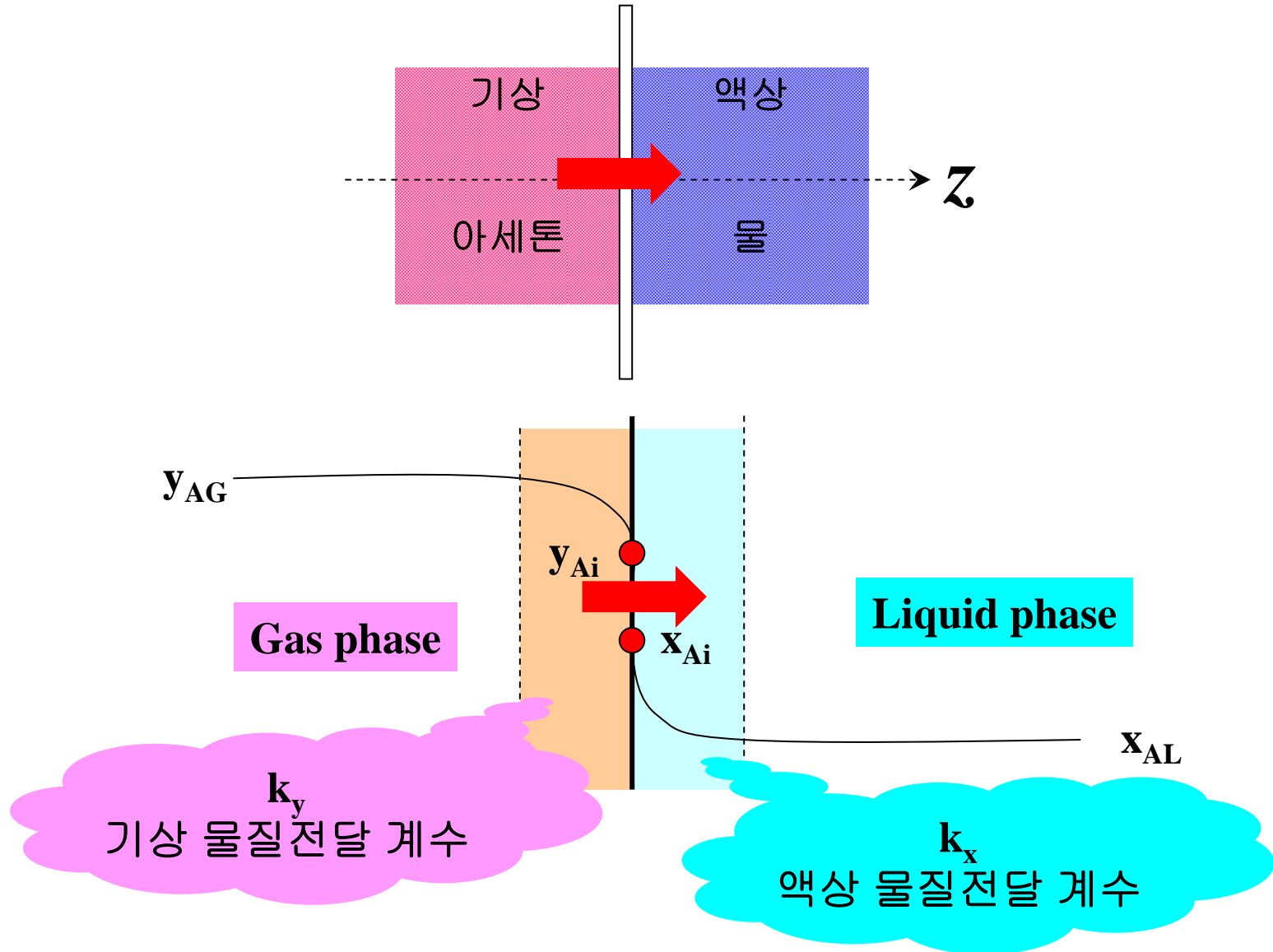
평판에 대한  
열전도와 열대류에 의한 총괄계수, U

$$q = \frac{1}{\frac{1}{h_i A} + \frac{\Delta x}{kA} + \frac{1}{h_o A}} (T_1 - T_4)$$

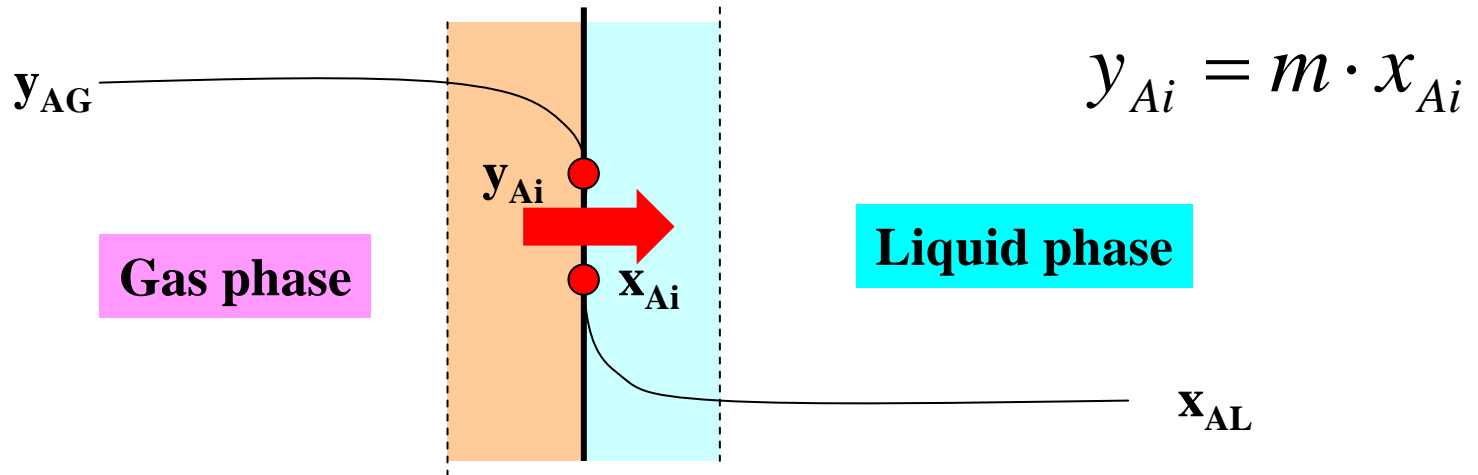
$$q = UA\Delta T$$

$$\text{where, } U = \frac{1}{\sum_i R_i} = \frac{1}{\frac{1}{h_i} + \frac{\Delta x}{k} + \frac{1}{h_o}}$$

# 10.4 두 상간의 물질전달



# 10.4 두 상간의 물질전달



$$N_A = N_{AG} = N_{AL}$$

$$y_{AG} - y_{Ai} = \frac{N_A}{k_y}$$

$$N_{AG} = k_y (y_{AG} - y_{Ai})$$

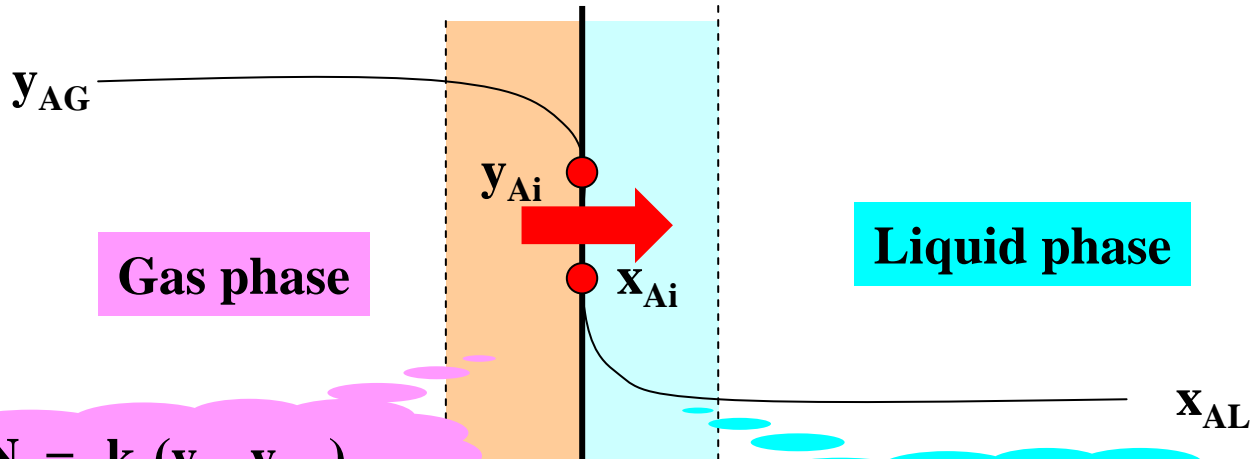
$$x_{Ai} - x_{AL} = \frac{N_A}{k_x}$$

$$N_{AL} = k_x (x_{Ai} - x_{AL})$$

$$N_A = \frac{1}{1/k_y + 1/k_x} (y_{AG} - m \cdot x_{AL})$$



# 10.4 두 상간의 물질전달



$$N_A = -k_y(y_{Ai} - y_{AG})$$

$$N_A = -k_x(x_{AL} - x_{Ai})$$

$$N_A = -D_A \frac{dC_A}{dx} + v_{bulk} C_A$$

$$N_A = -D_A \frac{dC_A}{dx} + \frac{C_A}{C_A + C_B} (N_A + N_B)$$

$$N_A = \frac{c_{total} D_{AB}}{(z_2 - z_1)} \ln\left(\frac{1 - y_{Ai}}{1 - y_{AG}}\right)$$

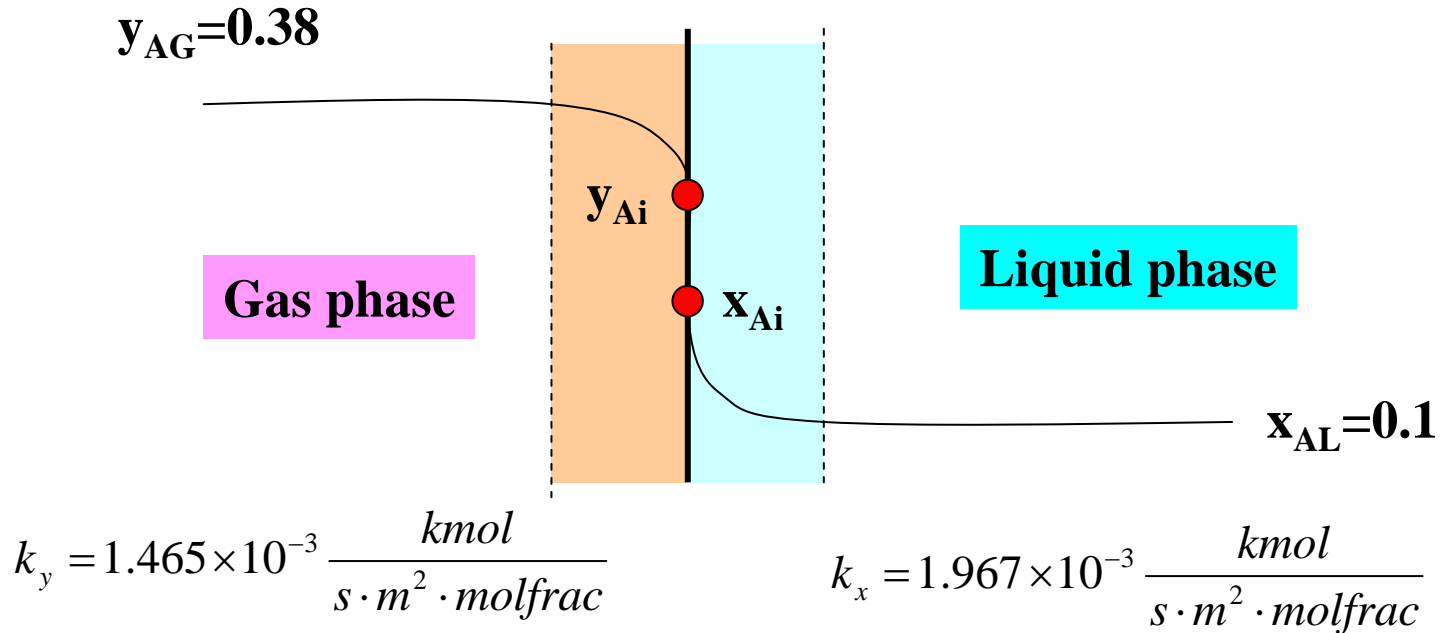
$$N_A = \frac{c_{total} D_{AB}}{(z_2 - z_1)} \ln\left(\frac{1 - y_{Ai}}{1 - y_{AG}}\right) \frac{y_{AG} - y_{Ai}}{(1 - y_{Ai}) - (1 - y_{AG})}$$

$$N_A = k'_y \frac{y_{AG} - y_{Ai}}{(1 - y_A)_{lm}}$$

확산항

대류항

# 예제 10.4-1 두 상간의 물질전달



$$y_A^* = 0.7 x_A^*$$

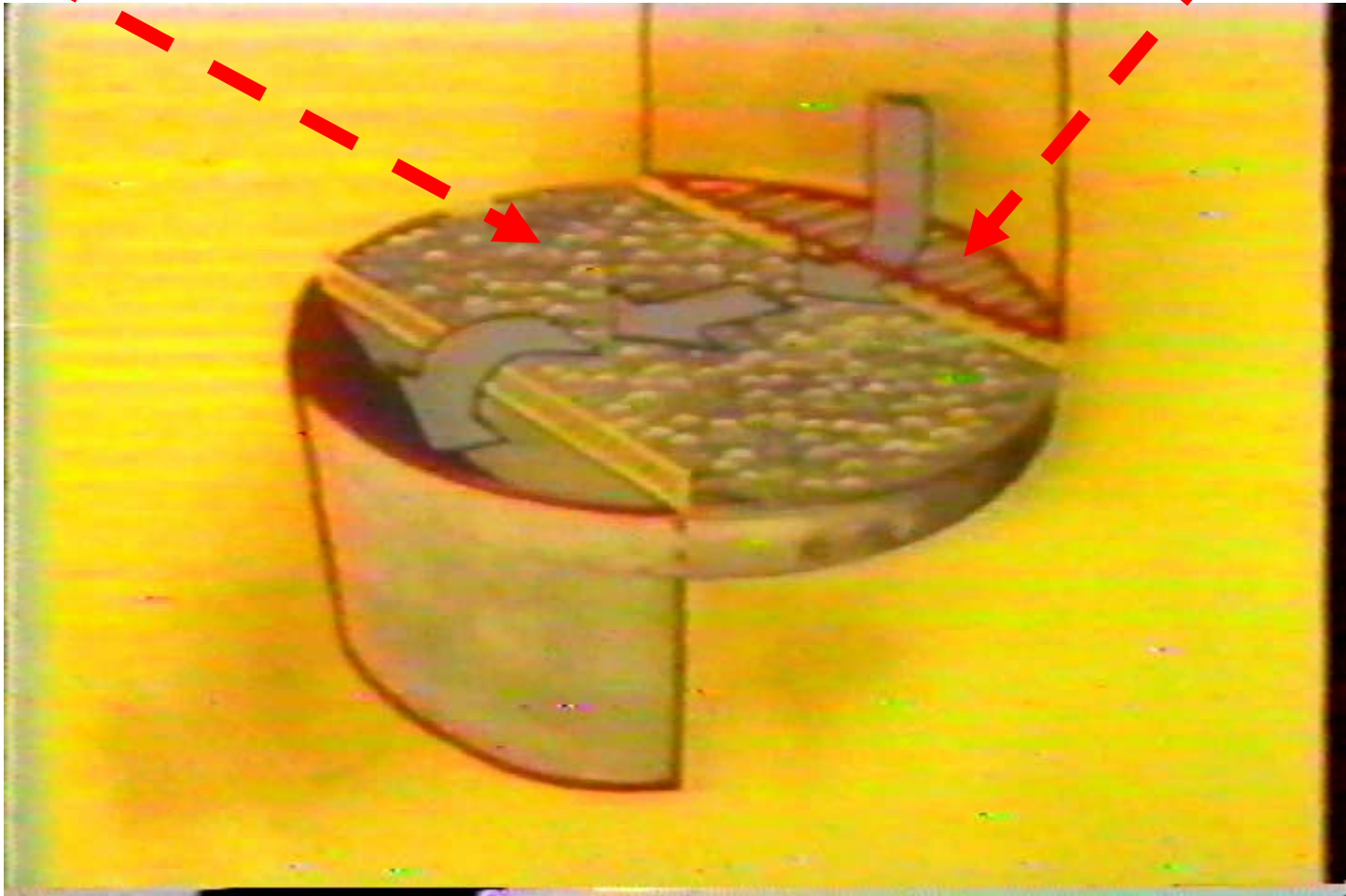
$$x_{Ai} = 0.257$$

$$N_A = ?$$

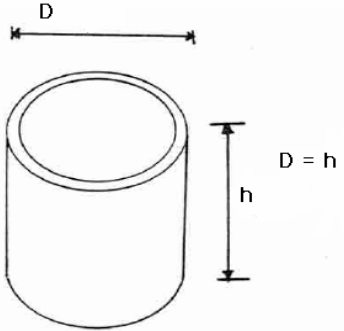
# 10.6 흡수탑/증류탑

Tray, bubbling area

downcommer



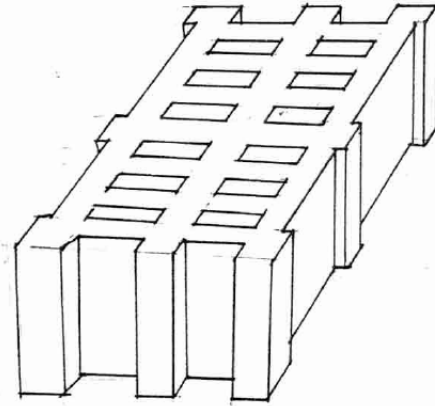
# 흡수탑에서의 충전물질



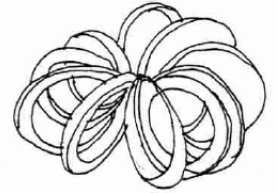
Resching Ring



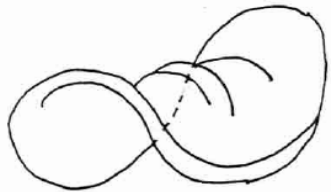
Rassing Ring



Grid Packing



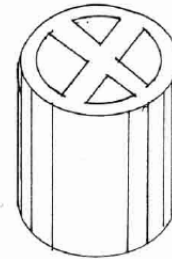
Tellerette



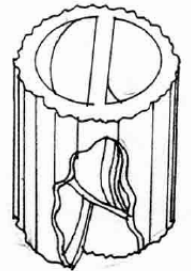
Berl saddle



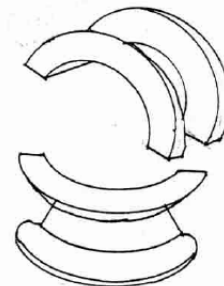
Pall Ring



Cross Partition Ring

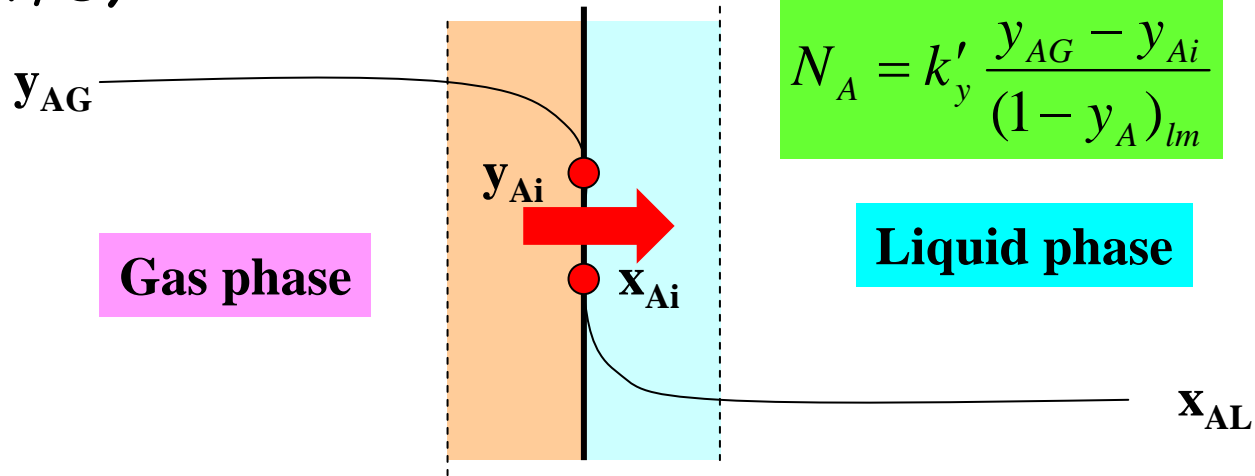
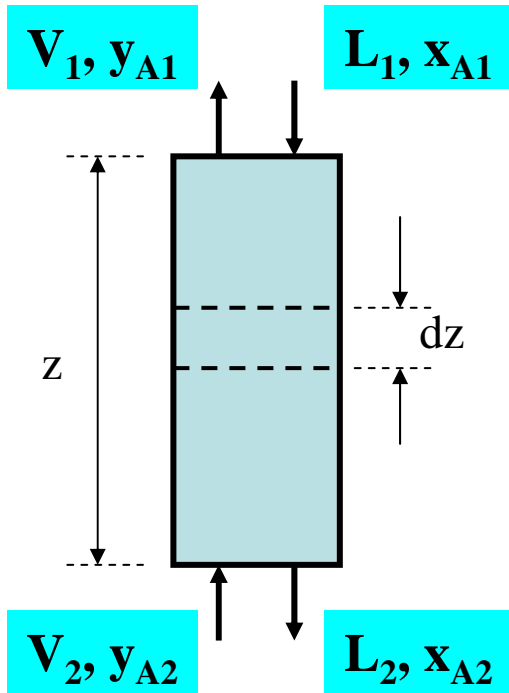


Cyclohelix Spiral Ring



Intalox Saddle

# 10.6 흡수탑 설계(1/5)



**흡수탑에서의 질량 보존**

1. 기상의 물질이 잃은 유량 ( $Q_V$ )
2. 액상의 물질이 얻은 유량 ( $Q_L$ )
3. 두 상간 전달된 유량 ( $Q_t$ )

**$Q_V = Q_L = Q_t$**

**열교환기에서의 에너지 보존**

1. 뜨거운 액체가 잃은 열량 ( $q_h$ )
2. 차가운 액체가 얻은 열량 ( $q_c$ )
3. 두 액체간 전달된 열량 ( $q_t$ )

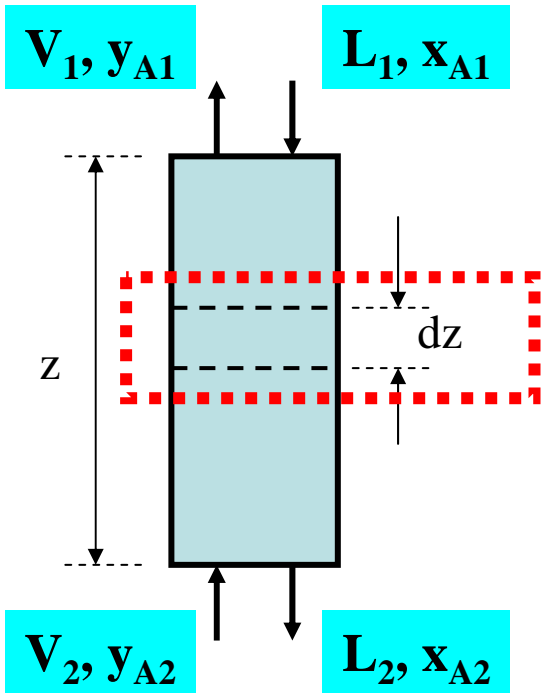
**$q_h = q_c = q_t$**

$$Q_V = V_2 y_{A2} - V_1 y_{A1}$$

$$Q_L = L_1 x_{A1} - L_2 x_{A2}$$

$$Q_t = N_A A = A \cdot k'_y \frac{y_{AG} - y_{Ai}}{(1 - y_A)_{lm}}$$

# 10.6 흡수탑 설계(2/5)



## 흡수탑에서의 질량 보존

1. 기상의 물질이 잃은 유량 ( $Q_V$ )
2. 액상의 물질이 얻은 유량 ( $Q_L$ )
3. 두 상간 전달된 유량 ( $Q_t$ )

$$Q_V = Q_L = Q_t$$

$$Q_V = V_2 y_{A2} - V_1 y_{A1}$$

$$Q_L = L_1 x_{A1} - L_2 x_{A2}$$

$$Q_t = N_A A = A \cdot k'_y \frac{y_{AG} - y_{Ai}}{(1 - y_A)_{lm}}$$

$$V(1 - y_A) = V'$$

$$dQ_V = d(Vy_A)$$

$$dQ_L = d(Lx_A)$$

$$dQ_t = N_A dA = k'_y \frac{y_A - y_{Ai}}{(1 - y_A)_{lm}} \cdot dA$$

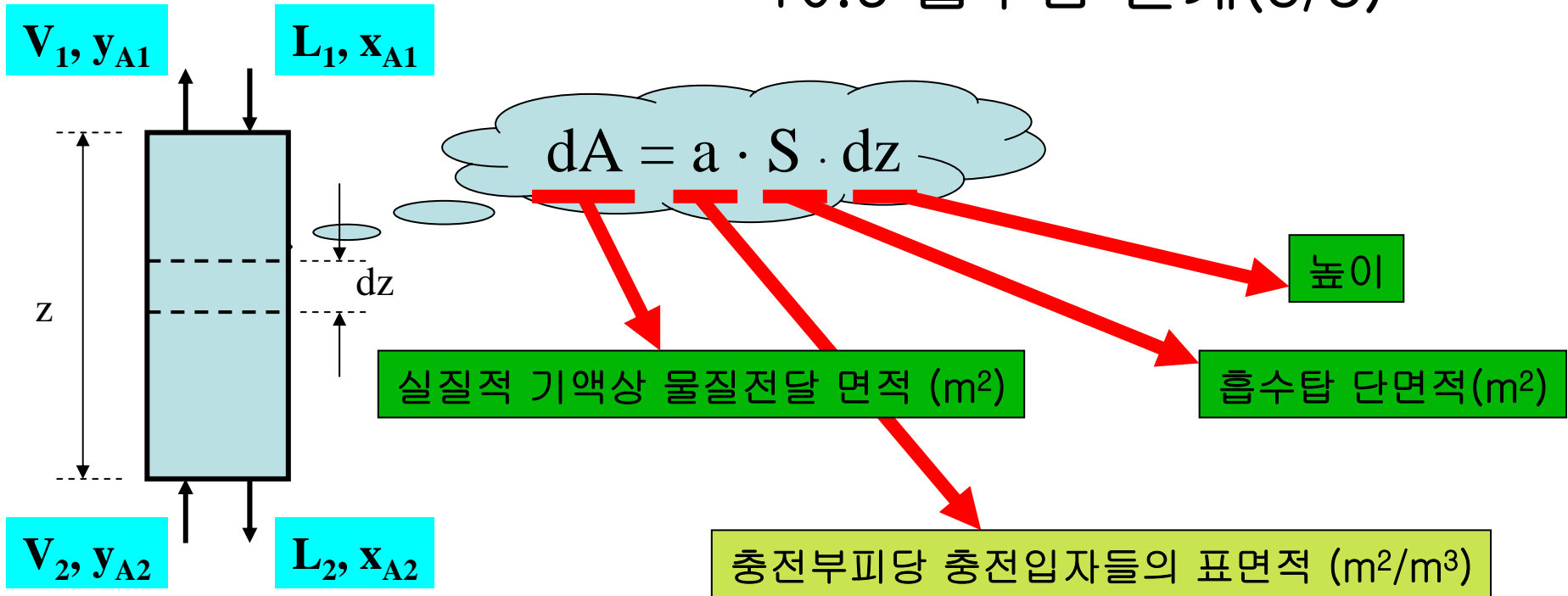
$$dQ_V = d(Vy_A) = \frac{V dy_A}{1 - y_A}$$

$$dQ_L = \frac{L dx_A}{1 - x_A}$$

$$dQ_t = k'_y \frac{y_A - y_{Ai}}{(1 - y_A)_{lm}} \cdot a S dz$$

$$dA = a S dz$$

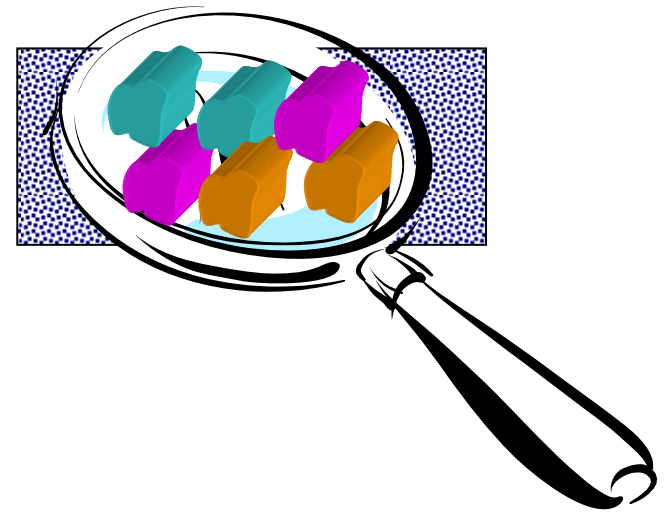
# 10.6 흡수탑 설계(3/5)



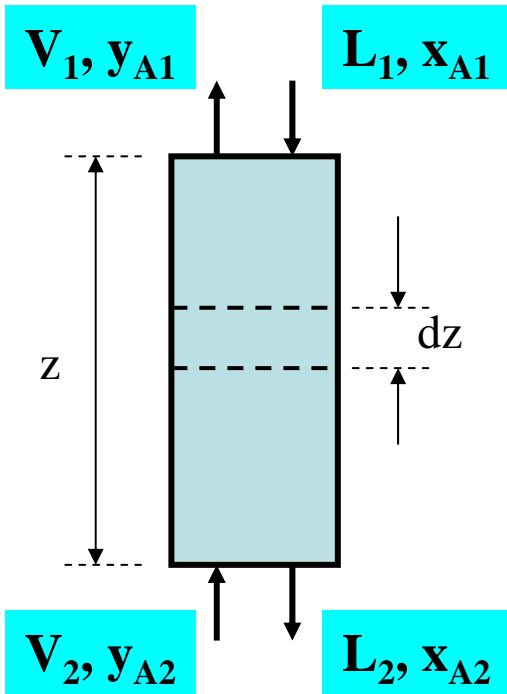
$$dQ_V = d(Vy_A) = \frac{Vdy_A}{1-y_A}$$

$$dQ_L = \frac{Ldx_A}{1-x_A}$$

$$dQ_t = k'_y \frac{y_A - y_{Ai}}{(1-y_A)_{lm}} \cdot aSdz$$



# 10.6 흡수탑 설계(4/5)



$$\frac{V dy_A}{1 - y_A} = k'_y \frac{y_A - y_{Ai}}{(1 - y_A)_{lm}} \cdot a S dz$$

$$\int_0^z dz = \int_{y_0}^y \left( \frac{(1 - y_A)_{lm}}{(1 - y_A) \cdot (y_A - y_{Ai})} \cdot \frac{V}{k'_y \cdot a \cdot S} \right) dy_A$$

$$z = \int_{y_0}^y \left( \frac{(1 - y_A)_{lm}}{(1 - y_A) \cdot (y_A - y_{Ai})} \cdot \frac{V}{k'_y \cdot a \cdot S} \right) dy_A$$

$$dQ_V = d(Vy_A) = \frac{V dy_A}{1 - y_A}$$

$$dQ_t = k'_y \frac{y_A - y_{Ai}}{(1 - y_A)_{lm}} \cdot a S dz$$

$$z = \frac{V}{k'_y \cdot a \cdot S} \cdot \frac{(1 - y_A)_{lm}}{(1 - y_A)} \int_{y_0}^y \frac{dy_A}{(y_A - y_{Ai})}$$

$$\frac{V}{S} (y_{A1} - y_{A2}) = k'_y \cdot a \cdot z \cdot (y_A - y_{Ai})_{lm}$$

Vapor mass flux

mass transfer flux



# 2004년 9월 5일 화공기사시험

- 문제 60: 도관의 내경이 49mm 이고 외경이 149mm 이며, 길이가 10m 일때, 이도관의 대수 평균표면적은?

가. 2.35 m<sup>2</sup>

나. 2.54 m<sup>2</sup>

다. 2.82 m<sup>2</sup>

라. 2.92 m<sup>2</sup>

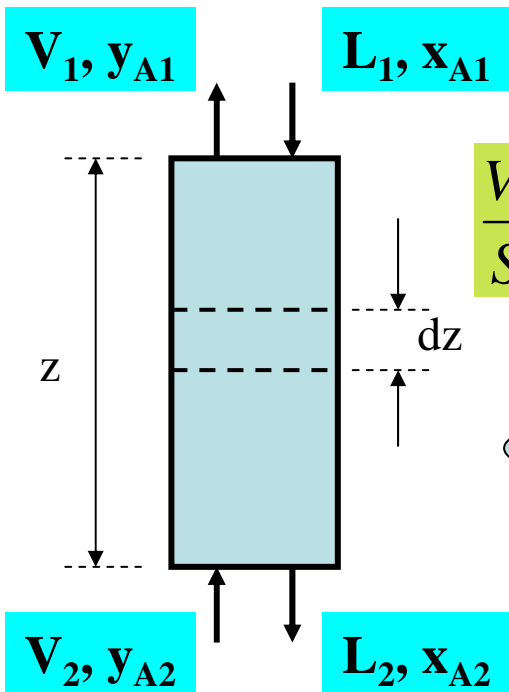
$$A_{\log mean} = \frac{A_2 - A_1}{\ln \frac{A_2}{A_1}}$$

$$A_2 = 2\pi r_2 L = \pi D_2 L = 3.14 \cdot 0.149 \cdot 10 = 4.68$$

$$A_1 = 2\pi r_1 L = \pi D_1 L = 3.14 \cdot 0.049 \cdot 10 = 1.54$$

$$A_{\log mean} = \frac{4.6786 - 1.5386}{\ln \frac{4.6786}{1.5386}} = 2.823$$

# 10.6 흡수탑 설계(5/5)



$$\frac{V}{S} (y_{A1} - y_{A2}) = \underbrace{k'_y \cdot a \cdot z}_{\text{Vapor phase}} \cdot (y_A - y_{Ai})_{lm} = \underbrace{k'_x \cdot a \cdot z}_{\text{Liquid phase}} \cdot (x_{Ai} - x_A)_{lm}$$

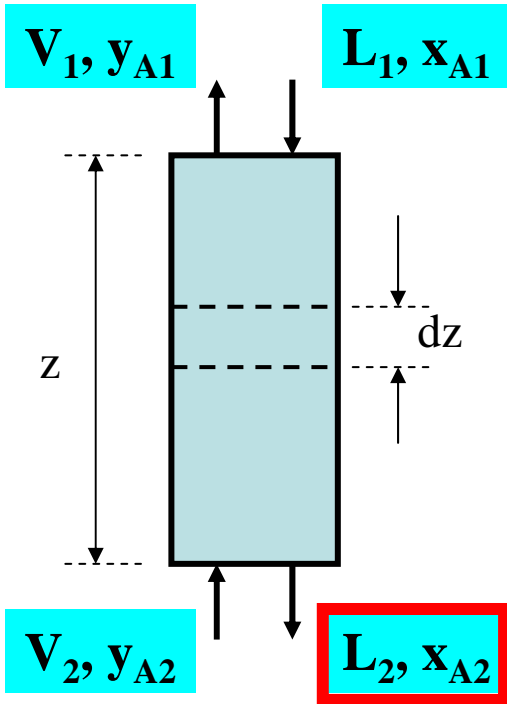
mass transfer flux:  
Vapor phase

mass transfer flux:  
Liquid phase

$$(y_A - y_{Ai})_{lm} = \frac{(y_{A1} - y_{Ai1}) - (y_{A2} - y_{Ai2})}{\ln \frac{(y_{A1} - y_{Ai1})}{(y_{A2} - y_{Ai2})}}$$

- 가정:
1. 희석기체 혼합물의 흡수이고 (몰분율이 10% 미만),
  2. 조업선과 평형선이 직선으로 간주할 수 있으며,
  3.  $(1-y_A)_{lm}/(1-y) \approx 1$  으로 간주할 때

# 예제: 10.6-2 아세톤 흡수탑



$$S=0.186\text{m}^2$$

$$T=293\text{K}, P=1\text{atm}$$

$$V'=13.65\text{kmol/h (air)}, y_{A2}=0.06, y_{A1}=0.005$$

$$L_1=45.36\text{kmol/h (water)}, x_{A1}=0$$

$$k_y'a=0.0378\text{kmol/s/m}^3$$

$$k_x'a=0.0616\text{kmol/s/m}^3$$

$$y=1.186x$$

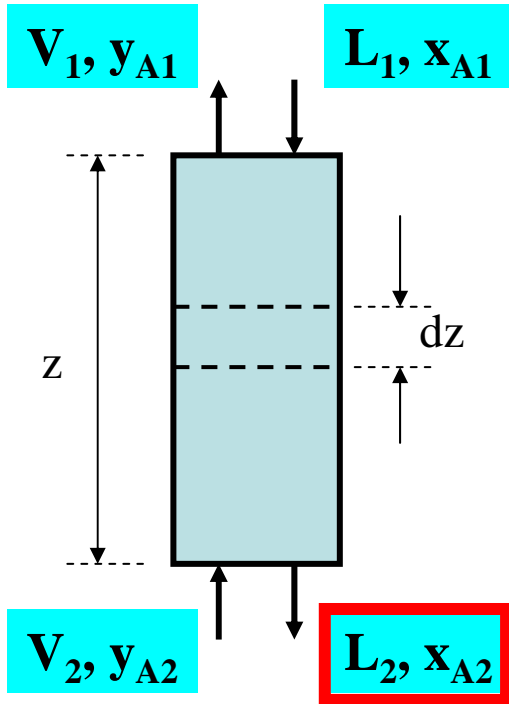
문제:

- 1) 평형단수는 몇 단인가?
- 2) 탑의 높이를 계산하시오.

계산순서

- 1) 미지수 ( $V_1, V_2, L_2, x_{A2}$ ) 를 구한다.
- 2) 조업선과 평형선을 그린다.
- 3) 평형단수를 구한다.
- 4) 평형농도값을 구한다 ( $y_{Ai1}, y_{Ai2}$ ) 를 구한다.
- 5) 식 (10.6-26) 을 이용하여  $z$  를 구한다.

# 예제: 10.6-2 아세톤 흡수탑



$$S=0.186\text{m}^2$$

$$T=293\text{K}, P=1\text{atm}$$

$$V'=13.65\text{kmol/h (air)}, y_{A2}=0.06, y_{A1}=0.005$$

$$L_1=45.36\text{kmol/h (water)}, x_{A1}=0$$

$$k'_y a=0.0378\text{kmol/s/m}^3$$

$$k'_x a=0.0616\text{kmol/s/m}^3$$

$$y=1.186x$$

$$\text{slope} = -\frac{k'_x a / (1 - x_1)}{k'_y a / (1 - y_1)}$$

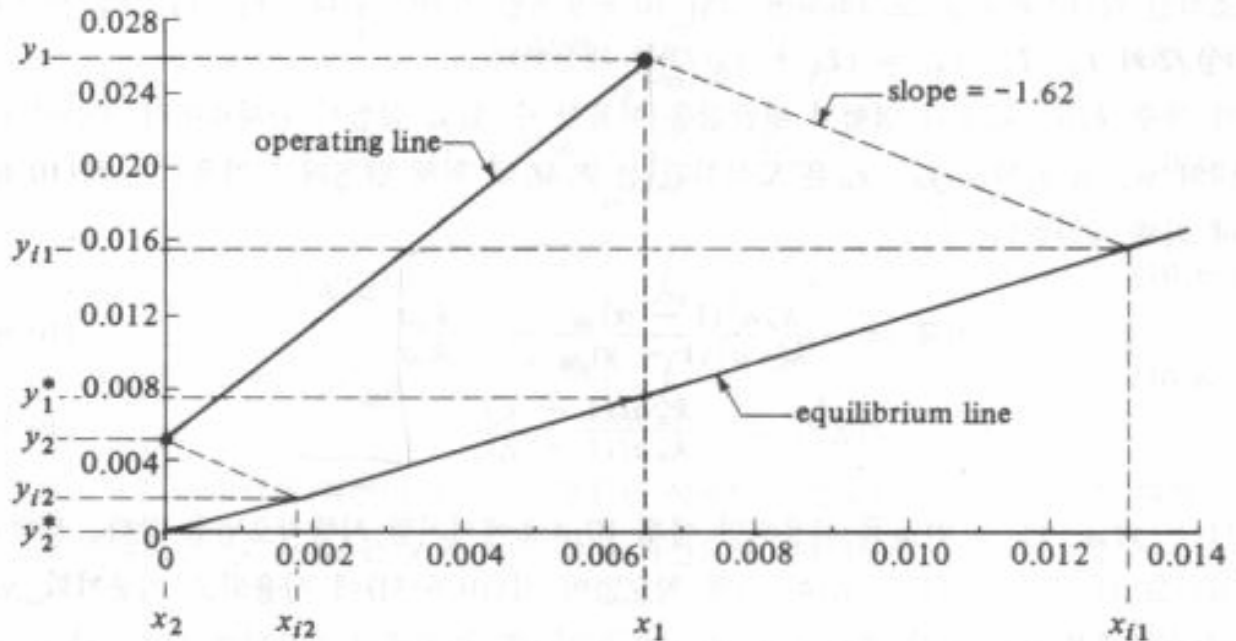


FIGURE 10.6-10. Location of interface compositions for Example 10.6-2.

## 과제 2. 흡수탑 (10.2-4, 10.6)

- 10.2-1
- 10.2-3
- 10.3-1
- 10.6-6 (a)
- 10.6-8: 평형식;  $y=0.039x$ ,  
예제 10.8-1 참조 (696쪽)